

X-RAY EMISSION FROM THE OLD PULSAR B0950+08

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ABSTRACT

We present the timing and spectral analyses of the *XMM-Newton* data on the 17 Myr old, nearby radio pulsar B0950+08. This observation revealed pulsations of the X-ray flux of PSR B0950+08 at its radio period, $P \simeq 253$ ms. The pulse shape and pulsed fraction are apparently different at lower and higher energies of the observed 0.2–10 keV energy range, which suggests that the radiation cannot be explained by a single emission mechanism. The X-ray spectrum of the pulsar can be fitted with a power-law model with a photon index $\Gamma = 1.75 \pm 0.15$ and an (isotropic) luminosity $L_X = (9.8 \pm 0.2) \times 10^{29}$ ergs s⁻¹ in the 0.2–10 keV range. Better fits are obtained with two-component, power-law plus thermal models with $\Gamma = 1.30 \pm 0.10$ and $L_X = (9.7 \pm 0.1) \times 10^{29}$ ergs s⁻¹ for the power-law component, which presumably originates from the pulsar’s magnetosphere. The thermal component, dominating at $E \lesssim 0.7$ keV, can be interpreted as radiation from heated polar caps on the neutron star surface covered with a hydrogen atmosphere. The inferred effective temperature, radius, and bolometric luminosity of the polar caps are $T_{PC} \approx 1$ MK, $R_{PC} \approx 250$ m, and $L_{PC} \approx 3 \times 10^{29}$ ergs s⁻¹. Optical through X-ray nonthermal spectrum of the pulsar can be described as a single power law with $\Gamma = 1.3$ –1.4 for the two-component X-ray fit. The ratio of the nonthermal X-ray (1–10 keV) luminosity to the nonthermal optical (4000–9000 Å) luminosity, ≈ 360 , is within the range of 10^2 – 10^3 observed for younger pulsars, which suggests that the magnetospheric X-ray and optical emissions are powered by the same mechanism in all pulsars, independent of age and spin-down power. Assuming a standard neutron star radius, the upper limit on the temperature of the bulk of the neutron star surface, inferred from the optical and X-ray data, is about 0.15 MK. We also analyze X-ray observations of several other old pulsars, B2224+65, J2043+2740, B0628–28, B1813–36, B1929+10, and B0823+26, and compare their properties with those of PSR B0950+08.

Subject headings: pulsars: individual (B0628–28, PSR B0823+26, PSR B0950+08, B1813–36, PSR B1929+10, PSR B2224+65, PSR J2043+2740) — stars: neutron — X-rays: stars

1. INTRODUCTION

Radiation from spin-powered pulsars at X-ray through optical wavelengths consists of thermal and nonthermal components (see Kaspi et al. 2004 for a recent review). In very young pulsars with characteristic ages $\tau = P/(2\dot{P}) \lesssim 10$ kyr (P and \dot{P} are the pulsar’s spin period and its derivative), such as the Crab pulsar, PSR B1509–58, and PSR B0540–69, thermal radiation from the neutron star (NS) surface is buried under a powerful nonthermal component from the NS magnetosphere, whose spectrum can be described by a power-law (PL) model, sometimes with a slowly varying slope. The luminosity of the magnetospheric component decreases with a pulsar’s age faster than the thermal luminosity (at $\tau \lesssim 1$ Myr), so that the thermal component, with typical surface temperatures of ~ 0.5 –1 MK, dominates in the X-ray (and, sometimes, far-UV) emission from middle-aged pulsars ($\tau \sim 0.01$ –1 Myr; e.g., PSRs B0656+14, B1055–52, J0538+2817, Vela, and Geminga—see Pavlov et al. 2002; Zavlin & Pavlov 2004). Old ($\tau \gtrsim 1$ Myr) NSs cool down very fast (unless a heating process operates in the NS interiors), so that the bulk of their surface radiation is emitted at optical-UV wavelengths. However, as predicted by virtually all pulsar models, small spots around the NS magnetic poles can be heated up to X-ray temperatures by relativistic particles generated in the pulsar acceleration zones. These polar caps (PCs) are too small to be detectable in the optical, but they can

be seen in soft X-rays. Whether the PC emission can be detected in X-rays, and the bulk surface emission detected in the optical, depends on the intensity of the magnetospheric component, which is rather poorly investigated because old pulsars are very faint objects beyond the radio band. Thus, studying the X-ray and optical emission from old pulsars allows one to understand evolution of the magnetospheric radiation at large ages and low spin-down energy losses, constrain the pulsar models through observations of PCs, and constrain the internal heating mechanisms through observations of thermal emission from the NS surface.

Similar problems have been addressed in X-ray and UV observations of the nearest millisecond (recycled) pulsar J0437–4715 ($P \simeq 6$ ms, $\tau \simeq 5$ Gyr, $d \simeq 140$ pc). Observations with *ROSAT* and *Chandra* have shown that its PC emission dominates in soft X-rays, while the magnetospheric radiation is responsible for the hard X-ray tail at $E \gtrsim 3$ keV (Zavlin & Pavlov 1998; Zavlin et al. 2002). Far-UV radiation from this pulsar shows a thermal spectrum emitted from the bulk of the NS surface with a temperature of ~ 0.1 MK (Kargaltsev et al. 2004). However, millisecond pulsars represent a separate class because they were spun up (recycled) by accretion in close binary systems. Their spin-down power, \dot{E} , is, as a rule, much higher than that of “ordinary” old pulsars, which can affect their magnetospheric emission. Heating mechanisms in these rapidly spinning objects can also be quite different. Therefore, ordinary old pulsars deserve a separate investigation.

Only two ordinary old pulsars, B1929+10 ($P = 0.226$ s, $\tau = 3.1$ Myr, $\dot{E} = 3.9 \times 10^{33}$ ergs s⁻¹) and B0950+08 ($P = 0.253$ s, $\tau = 17.4$ Myr, $\dot{E} = 5.6 \times 10^{32}$ ergs s⁻¹), were detected

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outside the radio band in the pre-*Chandra/XMM-Newton* era. For PSR B1929+10, *ROSAT* and *ASCA* observations provided some temporal and spectral information (Yancopoulos et al. 1994; Wang & Halpern 1997). Its X-ray light curve shows one broad pulse per period, with a pulsed fraction $f_p \approx 35\%$. The detected X-ray spectrum can be described by a PL model with a photon index $\Gamma \approx 1.8$. On the other hand, the same spectrum can be interpreted as thermal emission with a blackbody (BB) temperature $T_{\text{BB}}^{\infty} \approx 0.5$ MK and emitting area of $R_{\text{BB}}^{\infty} \approx 600$ m radius. The properties of the X-ray emission of PSR B0950+08 are even less certain. Although the pulsar was detected with *ROSAT* (Manning & Willmore 1994), the small number of source counts collected (~ 50) precluded a meaningful data analysis. PSR B0950+08 was also observed with *ASCA*, but it was unresolved from a brighter active galactic nucleus.

Both PSR B1929+10 and PSR B0950+08 were detected in the UV-optical by Pavlov et al. (1996) with the *Hubble Space Telescope (HST)* in a very broad band, $\approx 2400\text{--}4600$ Å. Further observations with narrower filters have shown that their optical radiation is likely of a nonthermal origin (Mignani et al. 2002; Zharikov et al. 2004). In particular, the *BVRI* spectrum of PSR B0950+08 was found to be consistent with a PL model with a broad range of photon indices, $\Gamma_{\text{opt}} = 1.25\text{--}2.05$. Because of the poor quality of the X-ray data available, the connection of the optical and X-ray spectra remained unclear.

The high sensitivity and spectral resolution of *Chandra* and *XMM-Newton* have provided new opportunities to study old pulsars. In this paper we present the analysis and interpretation of a recent *XMM-Newton* observation of PSR B0950+08, the oldest ordinary pulsar detected outside the radio wavelengths. We describe the *XMM-Newton* data in § 2 and present the results of our timing and spectral analysis in § 3. Interpretations of the broadband spectrum are discussed in § 4. In § 5 we compare the observed properties of PSR B0950+08 with the pulsar models and observations of other pulsars, including six old pulsars observed in X-rays. We summarize our results in § 6.

2. XMM-NEWTON OBSERVATION OF PSR B0950+08

XMM-Newton observed PSR B0950+08 on 2002 May 8–9 (orbit 442) for 83.9 and 58.0 ks effective exposures with the EPIC³-MOS and EPIC-pn instruments, respectively. For about 28 ks EPIC-MOS1 was operated in full-frame mode providing an image of a large area, $r \sim 14'$, with time resolution of 2.6 s. For the rest of the time it was in timing mode, which provides high time resolution of 1.5 ms at the expense of one dimension of the image. EPIC-MOS2 was in full-frame mode for the whole exposure. EPIC-pn was used in small-window mode, which covers a $4'37 \times 4'37$ region and provides a 5.7 ms time resolution. All the EPIC instruments were used with medium filters. Two reflection grating spectrometers (RGSs) observed the target in the standard spectroscopy mode for 84.4 ks.

Because of the high sensitivity and relatively high time resolution, the data collected with EPIC-pn are most suitable for studying the X-ray emission from PSR B0950+08. We used the EPIC-pn data processed with the most recent version of the SAS package⁴ (ver. 6.0.0). Time intervals with strong background flares at the beginning and the end of the observation were excluded, which, accounting for the 70% efficiency of

TABLE 1
OBSERVED PARAMETERS FOR THE RADIO PULSAR B0950+08

Parameter	Value
R.A. (J2000.0)	09 ^h 53 ^m 09 ^s .307(1)
Decl. (J2000.0).....	+07°55'36".15(2)
Epoch of position (MJD)	51,544.0
Proper motion in R.A./decl. (mas yr ⁻¹).....	-2.09(8)/29.46(7)
Spin frequency, f (Hz).....	3.951549502802(9)
Frequency derivative, \dot{f} (10 ⁻¹⁵ s ⁻²).....	-3.596(2)
Epoch of frequency (MJD)	52,403.0
Timing data span (MJD).....	52,280–52,630
Dispersion measure, DM (cm ⁻³ pc)	2.958(3)
Epoch of radio pulse (MJD TDB).....	52,402.848253347(2)
Distance, d (pc)	262(5)

NOTES.—Based on radio observations made at the Torun Radio Astronomy Observatory. The pulsar position, proper motion, and distance are from Brisken et al. (2002). The numbers in parentheses represent uncertainties in the least significant digit.

small-window mode, resulted in a 51.1 ks effective exposure. The pulsar is clearly detected in the EPIC-pn image at $\alpha = 09^{\text{h}}53^{\text{m}}09^{\text{s}}.34$ and $\delta = 07^{\circ}55'35''.2$ (J2000.0), which differs from the radio position (Table 1) by $1''.1$, well within the $2''\text{--}3''$ uncertainty of the EPIC absolute astrometry. The shape of the EPIC-pn image of the pulsar is consistent with that expected for a pointlike source. We put a 3σ upper limit of less than 2×10^{-14} photons s⁻¹ cm⁻² arcmin⁻² on the surface brightness of emission from a possible pulsar-wind nebula at distances $\sim 1'\text{--}2'$ from the pulsar.

We extracted the source (plus background) photons from a $30''$ radius circle centered at the pulsar position, which encircles about 82% of all detected source counts.⁵ For the analysis, we selected only single and double events (with photon-induced charge detected in a single CCD pixel and two adjacent pixels with horizontal or vertical splits) for which the instrumental response is known (those events provide about 98% of all detected photons). The extracted count rate spectrum shows strong excesses of single and double events at energies below 0.2 and 0.4 keV, respectively (see, e.g., van Kerkwijk et al. 2004), probably caused by the internal EPIC-pn “flickering.” Because the distribution of these detector background events is rather nonuniform over the field of view, they cannot be reliably subtracted; therefore, we had to discard single events with $E < 0.2$ keV and double events with $E < 0.4$ keV. The background was estimated from several circles of the same $30''$ radius centered at different positions. After the correction for the 82% encircled count fraction, we found the source count rate of 0.033 ± 0.001 counts s⁻¹ for single events in the 0.2–10 keV range. Adding doubles with $E > 0.4$ keV increases this value by 26%.

Because of the much lower sensitivity, the EPIC-MOS instruments detected the pulsar at a very low rate of about 0.007 counts s⁻¹. This makes the EPIC-MOS1 data hardly useful for the analysis because of a strong background contamination in timing mode (the same concerns are noted for the RGS data, where the source count rate is even smaller). We also do not use the EPIC-MOS data taken in the imaging mode because of uncalibrated changes in the low-energy spectral response of the EPIC-MOS detectors.⁶

³ European Photon Imaging Camera.

⁴ See <http://xmm.vilspa.esa.es>.

⁵ See the *XMM-Newton* Users' Handbook at <http://xmm.vilspa.esa.es>.

⁶ See <http://www.src.le.ac.uk/projects/xmm/technical/tuebingen0203.html>.

3. DATA ANALYSIS

3.1. Timing

For the pulsation search, we used 1568 events (singles and doubles) within the $r = 30''$ circle, in the 0.2–5.0 keV range, where the pulsar radiation prevails over the background. The source was estimated to contribute about 84% of the selected events. The photon times of arrival were transformed to the solar system barycenter with the *barycen* task of the SAS package. Using the TEMPO code,⁷ we calculated the radio ephemeris (see Table 1) based on observations of PSR B0950+08 in 2002 at the Torun Radio Astronomy Observatory (the data provided by W. Lewandowski). For the radio-pulsar frequency at the epoch of the *XMM-Newton* observation, the Z_n^2 test (e.g., Buccheri et al. 1983) yields values $Z_1^2 = 30.7$, $Z_2^2 = 61.4$, and $Z_3^2 = 72.7$, of which the latter is most significant; the probability to obtain this value by chance in one trial is 1.1×10^{-13} .

Using the radio data and the TEMPO code, we extracted the X-ray pulse profiles in radio phases ($\phi = 0$ corresponds to the phase of radio pulse maximum) from the single-event data in four energy ranges, 0.2–0.5, 0.5–1, 1–5, and 0.2–5 keV (see Fig. 1). At energies $E > 0.5$ keV (which contribute the bulk of the total detected emission) the light curves show two distinct peaks, centered at phases $\phi \approx 0.25$ and 0.85. The shapes of these peaks and the large pulsed fraction suggest a predominantly nonthermal origin of the pulsar emission at $E > 0.5$ keV. Interestingly, the separation $\Delta\phi \approx 0.4$ between the peaks is about the same as $\Delta\phi = 0.42$ between the radio pulse and interpulse, albeit the radio interpulse is a factor of 50 weaker than the main pulse (Everett & Weisberg 2001).

The shape of the light curve at lower energies looks different. The highest peak in the light curves at $E > 0.5$ keV (at $\phi \approx 0.25$) is strongly suppressed in the 0.2–0.5 keV pulse profile, so that the peak at $\phi \approx 0.85$ becomes dominant in this energy band. In addition, the pulsed fraction in the 0.2–0.5 keV band is reduced to about 33% (albeit with large uncertainties). To check whether the change in the shapes of the pulse profiles shown in the upper three panels of Figure 1 is statistically significant, we applied the χ^2 test as described by Zavlin & Pavlov (1998). This test gives a probability of 97.1% that the shapes of the light curves extracted in the 0.2–0.5 and 1–5 keV bands are different. The same test shows that the shapes of the 0.2–0.5 and 0.5–1 keV light curves differ with a probability of 94.7%. Therefore, it seems quite plausible that the change of the pulse shape and pulsed fraction is real. Since one can hardly expect significant changes of pulsations in a single nonthermal component over such a narrow energy range, we consider the apparent energy dependence of pulsations as an indication of the presence of another emission mechanism(s), with the main contribution at $E \lesssim 0.5$ keV.

3.2. Spectral Analysis of the Phase-integrated Spectrum

The EPIC-pn data on PSR B0950+08, reduced as described in § 2, were used for the spectral analysis. Because of the small number of counts collected, phase-resolved spectroscopy cannot produce useful results, so we have to use the phase-integrated spectrum. The EPIC-pn spectrum of the pulsar was binned in 32 spectral bins in the 0.2–10 keV range with at least 40 source counts per bin. This provides the signal-to-noise ratio $S/N = 5$ –6 in the spectral bins below 2 keV and $S/N =$

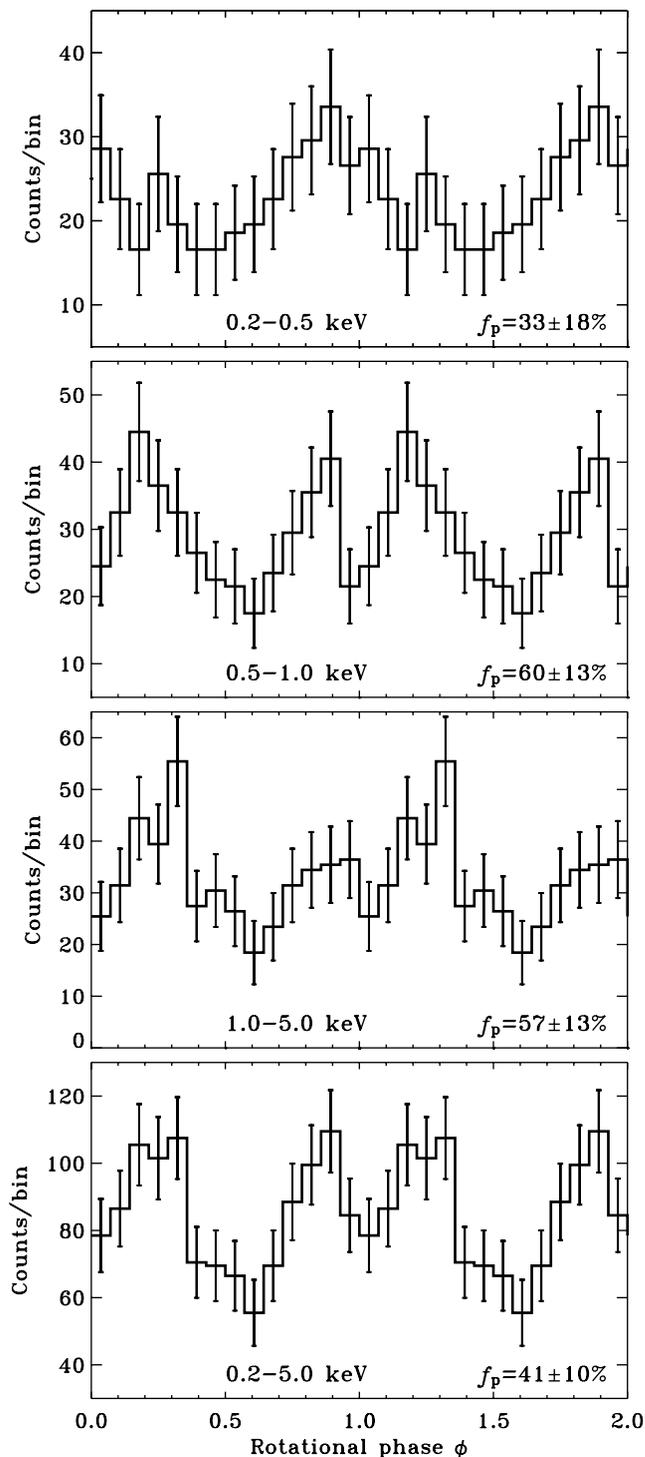


FIG. 1.—X-ray light curves of PSR B0950+08 extracted from the EPIC-pn data in four energy bands, with the values of the intrinsic pulsed fraction f_p and its 1σ errors. The zero phase corresponds to the maximum of radio pulse.

3.5–4 at $E > 2$ keV. We checked that varying the number of source counts per bin between 30 and 50 (with $S/N > 3$ in each of the spectral bins) makes no significant effect on the results presented below. We also verified that the 0.4–10 keV spectrum composed of double events is well consistent with that obtained from single events. Since the double-event spectrum is more noisy and contains only a quarter of the whole flux, we used only the single-event data for the further spectral analysis.

⁷ A program for the analysis of pulsar timing data maintained and distributed by Princeton University and the Australia Telescope National Facility. It is available at <http://www.atnf.csiro.au/research/pulsar/timing/tempo>.

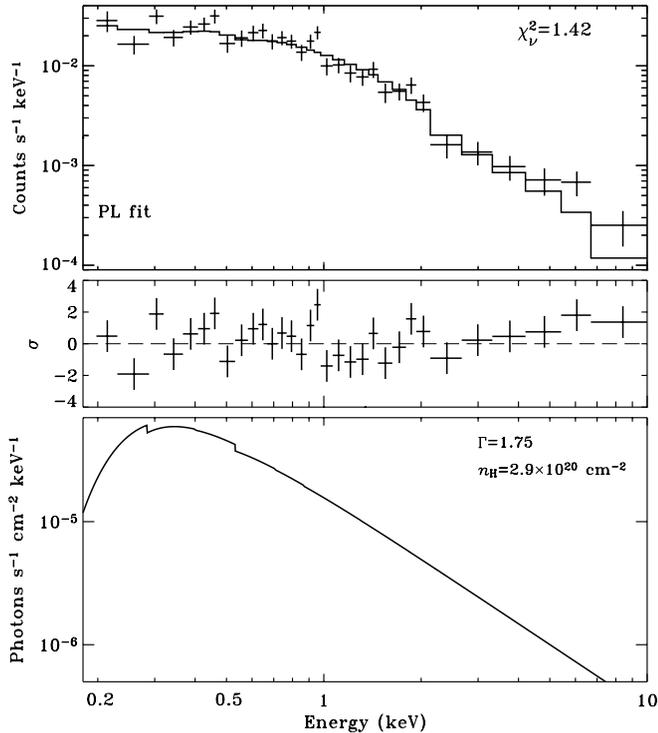


FIG. 2.—Observed EPIC-pn spectrum of PSR B0950+08 fitted with a single PL model of photon index $\Gamma = 1.75$ and residuals of the fit (top and middle panels). The model spectrum is shown in the bottom panel.

We started from fitting the pulsar count rate spectrum with one-component thermal models (BB and NS atmosphere) and found the best-fit models to be much softer than the data at $E \gtrsim 2$ keV, which resulted in an unacceptably large minimum χ^2_{ν} (>6.5 for $\nu = 29$ degrees of freedom [dof]). A fit with two thermal components (e.g., BB+BB) still has the same problem at $E \gtrsim 5$ keV. In addition, it yields an unreasonably high temperature, $T \gtrsim 10$ MK, and an unrealistically small size ($\lesssim 2$ m radius) for the harder component. This means that the observed spectrum at higher energies is of a nonthermal (presumably magnetospheric) origin, in agreement with the timing results (§ 3.1).

The (absorbed) PL model fits the data much better ($\chi^2_{\nu} = 1.42$ for 29 dof; see Fig. 2),⁸ yielding the photon index $\Gamma = 1.75 \pm 0.15$ and the absorbing hydrogen column density $n_{\text{H},20} \equiv n_{\text{H}}/(10^{20} \text{ cm}^{-2}) = 2.9 \pm 2.1$ (1 σ errors are given here and below). The observed (absorbed) flux in the 0.2–10 keV range, $F_{\text{X}} = (1.1 \pm 0.1) \times 10^{-13} \text{ ergs s}^{-1} \text{ cm}^{-2}$, corresponds to the (unabsorbed) isotropic luminosity⁹ $L_{2-10 \text{ keV}}^{\text{nonth}} = (9.8 \pm 0.2) \times 10^{29} \text{ ergs s}^{-1}$ and the “nonthermal X-ray efficiency” $\eta_{2-10 \text{ keV}}^{\text{nonth}} \equiv L_{2-10 \text{ keV}}^{\text{nonth}}/\dot{E} = (1.75 \pm 0.04) \times 10^{-3}$. Although the PL fit is (marginally) acceptable and the derived fitting parameters look reasonable, the fit residuals show that the model is somewhat softer than the data at $E \gtrsim 5$ keV (Fig. 2). This can be considered as an additional argument supporting the suggestion in § 3.1 that the X-ray emission of PSR B0950+08 consists of at least two components of different origin.

It is natural to assume (see § 1) that, in addition to the magnetospheric emission, thermal emission from heated PCs

contributes to the observed X-ray flux (see § 1). As a first step in the two-component, nonthermal plus thermal fit, we added a standard BB model to the PL component. The fit gives the BB temperature $T_{\text{BB}}^{\infty} = 1.75 \pm 0.22$ MK, effective radius $R_{\text{BB}}^{\infty} = 50 \pm 32$ m, and bolometric luminosity $L_{\text{BB}}^{\infty} = (1.6 \pm 0.8) \times 10^{29} \text{ ergs s}^{-1}$. [The superscript ∞ is used for the values as measured by a distant observer. The values as measured at the NS surface are $T_{\text{BB}} = g_r^{-1} T_{\text{BB}}^{\infty}$, $R_{\text{BB}} = g_r R_{\text{BB}}^{\infty}$, and $L_{\text{bol}}^{\text{PC}} = g_r^{-2} L_{\text{BB}}^{\infty}$, where $g_r = (1+z)^{-1} = (1-2GM/c^2R)^{1/2}$.] The PL photon index of the nonthermal component is $\Gamma = 1.31 \pm 0.14$, while the nonthermal luminosity, $L_{0.2-10 \text{ keV}}^{\text{nonth}} = (9.7 \pm 0.1) \times 10^{29} \text{ ergs s}^{-1}$, corresponds to the nonthermal X-ray efficiency $\eta_{0.2-10 \text{ keV}}^{\text{nonth}} = (1.73 \pm 0.02) \times 10^{-3}$. The hydrogen column density derived from the BB+PL fit, $n_{\text{H},20} = 3.3 \pm 2.2$, is almost the same as that obtained from the PL fit above, and it does not contradict independent estimates.¹⁰ The quality of the BB+PL fit, $\chi^2_{\nu} = 1.20$ for $\nu = 27$, is somewhat better than that obtained with the single PL model; however, according to the standard F -test, the probability that the spectral data require the second component is not very high, 96.1%.

The radius obtained from the BB+PL fit is much smaller than the expected PC radius, $\sim R(2\pi R/cP)^{1/2} = 288 (R/10 \text{ km})^{3/2}$ m. In addition, the isotropic BB emission from two symmetric PCs cannot reproduce the strong pulsations for realistic M/R ratio (e.g., Zavlin et al. 1995). However, the spectrum and the beaming of thermal emission can be substantially different from those of BB emission if the NS surface is covered by a light-element (hydrogen or helium) atmosphere (see Zavlin & Pavlov 2002 for a review on NS atmospheres). For example, if there is as little as 10^{13} g of hydrogen in the NS surface layers (e.g., as a result of accretion from the interstellar medium and/or fallback of a fraction of the envelope ejected during the supernova explosion), this hydrogen will rise to the surface forming an optically thick, purely hydrogen atmosphere. The spectrum emerging from a hydrogen atmosphere, which is almost fully ionized at the expected temperatures $\sim 10^6$ K and magnetic fields $\sim 10^{11}$ – 10^{12} G, is considerably harder at higher energies than the Planck spectrum with the same effective temperature, so that fitting the observed spectrum with a BB model gives a higher temperature and a smaller size, compared to their actual values (e.g., Pavlov et al. 1995). In addition, strong magnetic fields in NS atmospheres affect the beaming and the spectrum of the emergent radiation; in particular, the spectrum from a strongly ionized atmosphere shows an absorption line at the electron cyclotron energy $E_c = 1.16(B/10^{11} \text{ G})g_r$ keV.

To determine the effective temperature T_{PC} and the radius R_{PC} of PCs under the assumption of hydrogen atmosphere, we assume that the thermal X-rays are emitted from two similar, uniformly heated PCs around the magnetic poles of a centered magnetic dipole. In addition to the temperature and radius, the (phase-integrated) model spectrum depends on the magnetic field, inclination ζ of the rotation axis to the line of sight, magnetic inclination α between the magnetic and rotational axes, and the mass-to-radius ratio, M/R , which is responsible for the redshift and bending of photon trajectories in the strong gravitational field of the NS. Since a fit with so many fitting parameters would be essentially unconstrained, we have to

⁸ Systematic residuals at $E \lesssim 0.5$ keV can be attributed to uncertainties in the calibration of the EPIC-pn detector.

⁹ Here and below all the luminosities, efficiencies, and radii are given for a distance $d = 262$ pc (Briskin et al. 2002).

¹⁰ The total Galactic column density of neutral hydrogen along the direction to PSR B0950+08 is $n_{\text{H},20} \approx 3$ (<http://heasarc.gsfc.nasa.gov/cgi-bin/Tools/w3nh/w3nh.pl>). UV observations of stars at distances 110–160 pc from the pulsar give $n_{\text{H},20}$ in a range of 0.1–10, with large uncertainties (<http://archive.stsci.edu/cgi-bin/ismform>).

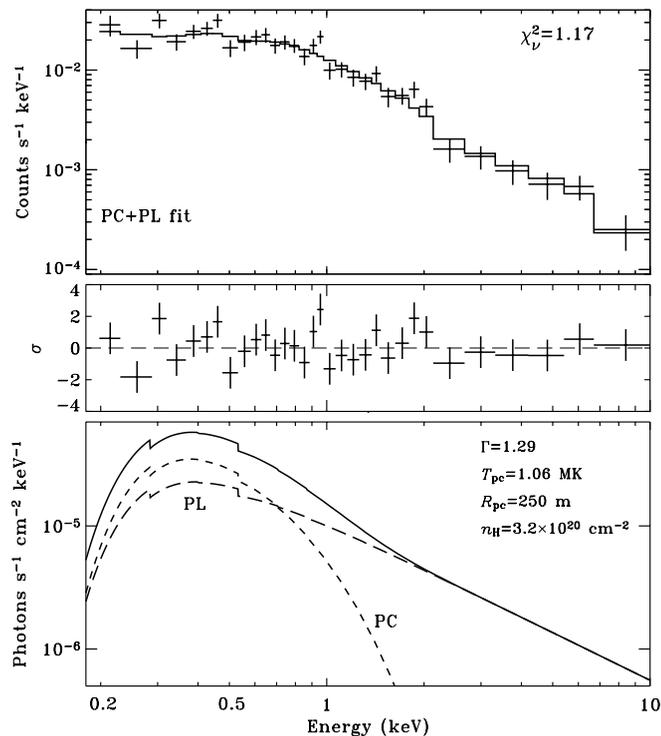


FIG. 3.—PC+PL fit to the observed EPIC-pn spectrum of PSR B0950+08 and its residuals (*top and middle panels*). The spectral components are shown in the lower panel. See § 3.2 for the other PC parameters.

choose fixed values for some of them. On the basis of the results of the single PL and BB+PL fits, we restricted the absorption column density in a plausible range, $2 < n_{\text{H},20} < 4$, chose, as an example, $B = 5 \times 10^{11}$ G (which is the magnetic field at the poles of an orthogonal rotator in the idealized magnetic dipole radiation model, $B_p = 6.4 \times 10^{19} [P\dot{P}]^{1/2}$ G), $\zeta = \alpha = 45^\circ$, $M = 1.4 M_\odot$, and $R = 10$ km ($g_r = 0.77$, $z = 0.30$). We calculated the model-specific intensities of emitted radiation on a T_{PC} grid and incorporated them in the XSPEC package. These intensities provide the spectra at different rotational phases as well as the phase-integrated spectrum (see Zavlin et al. 1995 and Zavlin & Pavlov 1998 for more details). The two-component (PC+PL) fit ($\chi_\nu^2 = 1.17$, for 27 dof) resulted in the PC (effective) temperature $T_{\text{PC}} = 1.06 \pm 0.16$ MK and radius $R_{\text{PC}} = 250 \pm 30$ m (as measured at the NS surface), the PL photon index $\Gamma = 1.29 \pm 0.12$, and $n_{\text{H},20} = 3.2 \pm 0.8$. Varying ζ and α between 0° and 90° and the mass-to-radius ratio in a plausible range of $M/R = (1.0\text{--}1.8) M_\odot / (10 \text{ km})$ changes the best-fit temperature by $\lesssim 0.1$ MK and the best-fit radius by $\lesssim 90$ m. The bolometric luminosity of the thermal component is $L_{\text{bol}}^{\text{PC}} = (2.7 \pm 0.8) \times 10^{29}$ ergs s^{-1} (for two PCs), while the nonthermal component has the same luminosity as the best BB+PL fit. The best PC+PL fit, together with the two spectral components, is shown in Figure 3. As seen from this plot, the thermal component dominates at $E < 0.7$ keV, providing about 60% of the total flux observed in the 0.2–0.5 keV range. We checked that varying the magnetic field has almost no effect on the inferred PC parameters as far as the cyclotron energy remains in the Wien tail, $B \gtrsim 2 \times 10^{11}$ G.

3.3. Thermal Light-Curve Analysis

The PC model used in § 3.2 for the analysis of the phase-integrated spectrum predicts a large variety in pulse profiles of the thermal emission, depending on the pulsar geometry, mass-

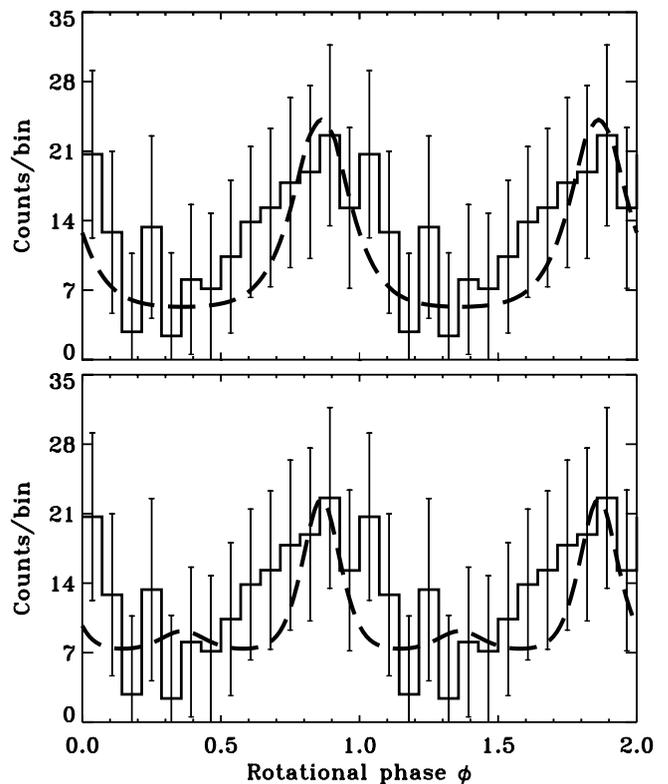


FIG. 4.—Residual pulse profile (*histograms*) in the 0.2–0.5 keV band after subtracting the scaled 1–5 keV light curve. Thick dashes show the pulse profiles for the PC models with the angles $\zeta = 35^\circ$, $\alpha = 30^\circ$ (*upper panel*), and $\zeta = 53^\circ$, $\alpha = 75^\circ$ (*lower panel*). See § 3.3 for the other PC parameters.

to-radius ratio, and surface magnetic field (Zavlin et al. 1995). Therefore, these parameters can be constrained from the comparison of the model light curves with the observed ones (cf. Pavlov & Zavlin 1997). To make such a comparison for PSR B0950+08, one first needs to single out the contribution of the possible thermal component in the observed light curve. Assuming that the pulse shape of the nonthermal flux does not depend on photon energy in the observed X-ray range, we scaled the nonthermal light curve of the 1–5 keV band (where the PC contribution is virtually negligible, $\lesssim 5\%$) to the 0.2–0.5 keV band, chosen for the thermal light-curve analysis, and subtracted the scaled nonthermal light curve. The scaling factor of 0.31 was estimated as the ratio of the number of counts provided by the nonthermal component of the best PC+PL fit of § 3.2 in the 0.2–0.5 keV band to the total number of counts in the 1–5 keV band (varying the parameters of the PL component within the 1σ confidence range changes this factor by 15% only, which makes a negligible effect on the results presented below). The result of the light-curve subtraction is shown in Figure 4. Although the residual pulse profile is noisy because of the scanty statistics, it shows a structure around the phase $\phi = 0.85$ that can be interpreted as a pulse of thermal emission. The pulsed fraction of this light curve is fairly large, with a lower limit of 35%. Such a high pulsed fraction cannot be obtained with the isotropic BB radiation for any ζ and α unless the NS mass-to-radius ratio is so (unrealistically) small, $(M/M_\odot)/(R/10 \text{ km}) \lesssim 0.25$ (i.e., gravitational redshift $z \lesssim 0.04$), that the effect of the gravitational bending is negligible. Therefore, a strong magnetic field, $B \gtrsim 10^{11}$ G, is required to explain the large pulsed fraction. In strong fields such that $E_c \gg E$, the angular distribution of the emergent radiation

shows a narrow beam along the direction of the magnetic field (where the atmospheric plasma is most transparent for radiation) and a rather broad hollow-cone beam around the magnetic field direction (Pavlov et al. 1994; Zavlin & Pavlov 2002). If ζ and α are such that the narrow beam passes through the line of sight in the course of pulsar rotation, the observed flux can be very strongly modulated.

Because of the large errors in the residual light curve shown in Figure 4, fitting it with the multiparameter PC models is hardly warranted. Instead, we crudely determined domains of parameters where this light curve qualitatively agrees with the models. For several sets of B , ζ , α , and M/R , we found best-fit T_{PC} , R_{PC} , and n_{H} from spectral fits (as described in § 3.2), used these values to compute the model fluxes as a function of phase, and folded these fluxes with the EPIC-pn response. Comparing the model light curves with the residual light curve, we found that a reasonably good agreement can be achieved, for example, in the following ranges of parameters: $|\zeta - \alpha| \lesssim 20^\circ$, $30^\circ \lesssim \zeta \lesssim 75^\circ$, $B \approx (2-3) \times 10^{11}$ G, and $(M/M_\odot)/(R/10 \text{ km}) \approx 1.2-1.6$. At larger $|\zeta - \alpha|$, the peak direction of the narrow beam (along the magnetic axis) remains too far from the line of sight, which results in low modulation of the model flux. The modulation is also too low at small ζ and/or α , while at ζ and α close to 90° we would see two peaks of comparable strength, in contradiction with the residual light curve. At higher magnetic fields, the central beam becomes too narrow, so that the pulse profiles with a sufficiently large pulsed fraction are sharper than observed. An example of a reasonably good agreement is shown in the upper panel of Figure 4 that presents a model light curve with $B = 2 \times 10^{11}$ G, $\zeta = 35^\circ$, $\alpha = 30^\circ$, and $[M/M_\odot]/[R/10 \text{ km}] = 1.4$ ($T_{\text{PC}} = 1.02$ MK, $R_{\text{PC}} = 280$ m, and $n_{\text{H},20} = 3.0$). The model pulsed fraction is $f_p = 68\%$.

In principle, independent estimates on the angles ζ and α can be obtained from the phase dependence of the position angle of the linearly polarized radio emission (Radhakrishnan & Cooke 1969). For PSR B0950+08, the estimates obtained by different authors are summarized by Everett & Weisberg (2001). Most of them suggest that PSR B0950+08 is an almost aligned rotator with only one pole visible: $\alpha \lesssim 12^\circ$, $\zeta \lesssim 5^\circ$. At such small angles, the pulsed fraction of the PC X-ray radiation, $f_p \lesssim 15\%$, is too low to be consistent with the residual light curve, even accounting for the uncertainty in the light-curve subtraction. The result of Everett & Weisberg (2001), $\zeta \simeq 53^\circ$ and $\alpha \simeq 75^\circ$ (an almost orthogonal rotator, with two poles visible) differs significantly from the others. The pulse profile for the PC model with these angles and $B = 2 \times 10^{11}$ G, $M = 1.4 M_\odot$, and $R = 10$ km ($T_{\text{PC}} = 1.05$ MK and $R_{\text{PC}} = 300$ m, $n_{\text{H},20} = 3.0$) is shown in the lower panel of Figure 4. Its pulsed fraction is $f_p = 54\%$. Although the agreement does not look as good as in the upper panel, the deviation from the observational light curve is well within the uncertainties.

4. X-RAYS VERSUS OPTICAL

The optical-UV fluxes measured in the *HST*, VLT, and *Subaru* observations of PSR B0950+08 (see Fig. 5) can be crudely described by a PL spectral model, with a photon index $\Gamma_{\text{opt}} = 1.65 \pm 0.40$ (Zharikov et al. 2004).¹¹ This means that both optical ($E \approx 1.5-5$ eV) and X-ray ($E \gtrsim 1$ keV) emission

¹¹ The value for Γ_{opt} was obtained neglecting the interstellar extinction. The large scatter of fluxes in the different optical bands and the resulting uncertainty of spectral slope are likely due to errors in subtraction of the flux of background objects near PSR B0950+08.

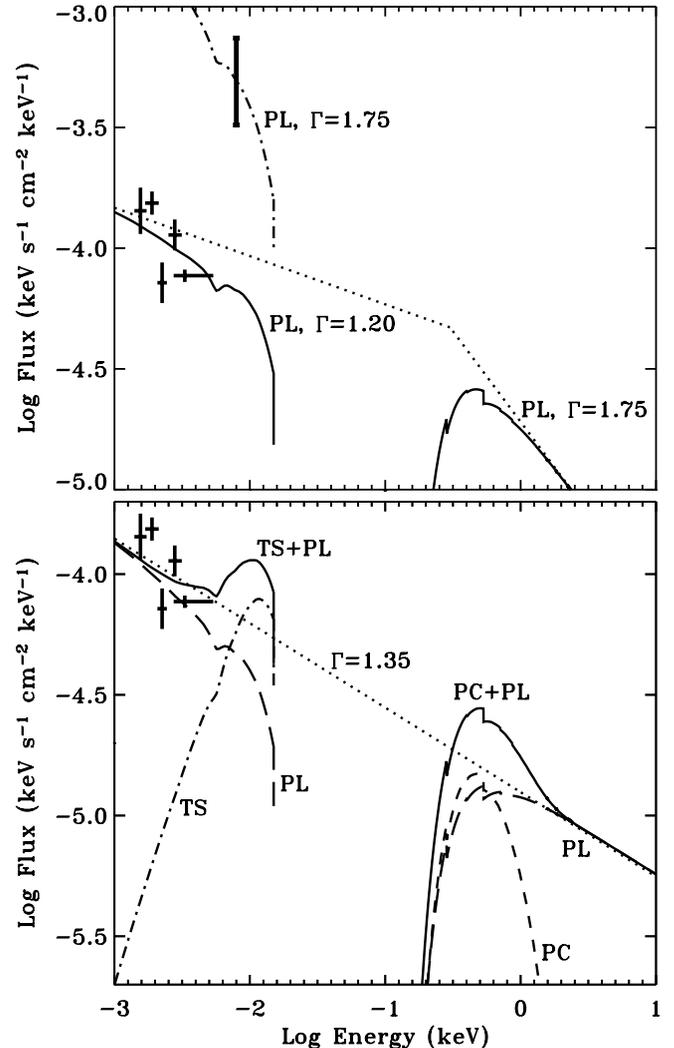


Fig. 5.—Broadband (optical through X-ray) spectrum of PSR B0950+08 for two models of its X-ray spectrum: single PL (upper panel) and PC+PL (lower panel). The model spectra are shown with the solid lines in the X-ray range; the PC model is the same as that used for modeling the pulse profile in the upper panel of Fig. 4. Crosses show the observed fluxes in optical-UV bands (Pavlov et al. 1996; Zharikov et al. 2004). The optical spectrum is modeled by an absorbed PL with $\Gamma = 1.20$ and 1.35 (solid and dashed lines in the upper and lower panels, respectively), and $E(B - V) = 0.05$. The dash-dotted line in the upper panel shows an extrapolation of the X-ray PL spectrum into the optical; the thick vertical bar demonstrates the propagated errors. The dotted lines show the unabsorbed spectra of the nonthermal components, single and broken PLs in the lower and upper panels, respectively. The solid line in the optical part of the lower panel shows the sum of the PL component and a possible thermal component (TS) from the whole NS surface, for a 0.1 MK temperature (see § 4 for other model parameters).

from PSR B0950+08 are nonthermal, most likely emitted by relativistic particles in the pulsar magnetosphere. From observations of younger pulsars, we know that the optical and X-ray parts of the nonthermal spectrum can be described by the same PL model for some of them (e.g., PSR B0656+14; see Pavlov et al. 2002), while in others the optical spectrum is harder than the X-ray spectrum (i.e., $\Gamma_{\text{opt}} < \Gamma_{\text{X}}$), and it lies below the extrapolation of the X-ray PL as, for example, in the Crab pulsar (Kuiper et al. 2001). The change of the spectral slope in the latter case can be attributed, for example, to deviation of the spectrum of emitting electrons from the pure PL or, less likely, to different populations of electrons emitting in the optical and X-ray bands.

The two possible interpretations of the X-ray spectrum of PSR B0950+08 (pure PL and PC+PL) correspond to the different broadband (optical through X-rays) spectra described above. The extrapolation of the single PL model with $\Gamma = 1.6\text{--}1.9$ toward lower energies exceeds the observed optical spectrum by a factor of 10–30, depending on Γ and optical frequency. In this case, we have to assume a change in the PL slope somewhere in the EUV or soft-X-ray range and a rather small $\Gamma_{\text{opt}} \lesssim 1.2$, as demonstrated in the upper panel of Figure 5. On the contrary, the extrapolation of the PL component of the PC+PL model, which we consider more plausible than the single PL model, goes through the optical points, so that the nonthermal spectrum in the 1 eV–10 keV range can be described by a single PL with $\Gamma = 1.3\text{--}1.4$. The lower panel of Figure 5 shows the broadband spectrum for $\Gamma = 1.35$; the corresponding broadband nonthermal luminosity is $L_{1\text{ eV--}10\text{ keV}}^{\text{nonth}} = 1.1 \times 10^{30} \text{ ergs s}^{-1} = 1.8 \times 10^{-3} \dot{E}$, of which the optical luminosity is a small fraction (e.g., $L_{1\text{--}5\text{ eV}} = 5.2 \times 10^{27} \text{ ergs s}^{-1} = 4.7 \times 10^{-3} L_{1\text{ eV--}10\text{ keV}}^{\text{nonth}}$).

Because of the small emitting area, the thermal PC radiation falls about 3 orders of magnitude below the detected optical fluxes. On the other hand, one cannot rule out the possibility that the bulk of the NS surface is hot enough to emit detectable thermal radiation. Assuming a constant slope of the optical through X-ray spectrum, we estimate an upper limit on the NS brightness temperature in the optical-UV: $T^{\infty} \lesssim 0.15 \text{ MK}$, for $R^{\infty} = 13 \text{ km}$ and a plausible optical extinction, $E(B - V) = 0.05$. This limit is much higher than the expected surface temperature of a 20 Myr old, passively cooling NS (Yakovlev & Pethick 2004). However, various processes of NS heating (see Schaab et al. 1999 for a review) can heat the surface up to even higher temperatures at this NS age. Kargaltsev et al. (2004) detected thermal emission from the much older ($\tau = 4.9 \text{ Gyr}$) millisecond pulsar J0437–4715, corresponding to the surface temperature of about 0.1 MK. Therefore, one could expect at least a similar surface temperature for the younger PSR B0950+08, unless millisecond pulsars are heated by a specific mechanism that does not work in ordinary pulsars (e.g., Reisenegger 1997). To illustrate the effect of such temperatures on the broadband spectrum of PSR B0950+08, we assumed a bulk surface temperature $T_s^{\infty} = 0.1 \text{ MK}$ and plotted the corresponding (BB) spectrum in the lower panel of Figure 5, for a NS radius $R^{\infty} = 13 \text{ km}$. This thermal component (the TS curve in Fig. 5) gives virtually no contribution into the observed X-ray range, but it would be observable in the far-UV range, at $\lambda \lesssim 2000 \text{ \AA}$.

5. DISCUSSION

5.1. Nonthermal Emission from PSR B0950+08 and Other Pulsars

Since the bulk of the X-ray and optical emission observed from PSR B0950+08 is nonthermal, it is interesting to compare it with the nonthermal emission from other spin-powered pulsars. We know from X-ray observations that the pulsar nonthermal luminosity shows a correlation with the spin-down power \dot{E} . For instance, Possenti et al. (2002) found a fit $L_{2\text{--}10\text{ keV}}^{\text{nonth}} = 3.6 \times 10^{31} (\dot{E}/10^{35} \text{ ergs s}^{-1})^{1.34} \text{ ergs s}^{-1}$, based on observations of 37 pulsars (mostly with *ROSAT*, *ASCA*, and *BeppoSAX*). However, the observed luminosities showed large deviations, up to 2 orders of magnitude, from this dependence. The scatter becomes even larger if one includes the upper limits for pulsars that were not detected in deep observations (see some examples in § 5.3). Such a scatter can be

naturally explained by geometrical factors. First, the actual luminosity can differ substantially from the “isotropic luminosity” $4\pi d^2 F_X^{\text{unabs}}$ because a pulsar’s X-ray radiation is anisotropic, as we see from their pulsations, and even powerful and radio-bright pulsars can be quite faint in X-rays if the rotating X-ray beam misses the Earth. Second, the properties of a pulsar’s magnetosphere and its radiation can strongly depend on the magnetic inclination α that is unknown for most pulsars. Therefore, more physical is the “line of maximum luminosity” in the $\dot{E}\text{--}L_X^{\text{nonth}}$ plane, such that all the observed luminosities lie below that line. The ratio $\eta_{\text{max}}^{\text{nonth}} \equiv L_{\text{max}}^{\text{nonth}}/\dot{E}$ characterizes maximum efficiency of conversion of the spin-down power into X-ray radiation. Possenti et al. (2002) suggested $\eta_{\text{max}}^{\text{nonth}} = 0.02 (\dot{E}/10^{35} \text{ ergs s}^{-1})^{0.48}$, in the 2–10 keV band, which implies that pulsars with low \dot{E} are less efficient X-ray emitters.

The derived luminosity of the nonthermal component of PSR B0950+08 in the 2–10 keV range is $L_{2\text{--}10\text{ keV}}^{\text{nonth}} \simeq 7.3 \times 10^{29} \text{ ergs s}^{-1}$, corresponding to $\eta_{2\text{--}10\text{ keV}}^{\text{nonth}} = 0.0013$. These values exceed by a factor of 20 the prediction of the $L_X^{\text{nonth}}\text{--}\dot{E}$ correlation derived by Possenti et al. (2002), being close to the maximum values, $L_{\text{max}}^{\text{nonth}} = 9.3 \times 10^{29} \text{ ergs s}^{-1}$ and $\eta_{\text{max}}^{\text{nonth}} = 0.0017$.

It is worthwhile to note that the nonthermal X-ray luminosity of PSR B0950+08 is only a factor of 2 lower than that of the much more powerful ($\dot{E} = 3.8 \times 10^{34} \text{ ergs s}^{-1}$) middle-aged ($\tau = 110 \text{ kyr}$) pulsar B0656+14 (Pavlov et al. 2002), which means that PSR B0656+14 is a factor of 30–40 less efficient nonthermal X-ray emitter than PSR B0950+08. Even less efficient, by a factor of about 600 with respect to PSR B0950+08, is the younger ($\tau = 11 \text{ kyr}$) Vela pulsar (Pavlov et al. 2001). On the basis of these examples, it might be tempting to speculate that the nonthermal X-ray efficiency grows with decreasing \dot{E} or increasing τ . However, there are many other middle-aged pulsars whose efficiency is much higher than that of PSR B0656+14 or Vela, even with account for larger uncertainties in their distances. Therefore, the most plausible reason for the high nonthermal X-ray efficiency of PSR B0950+08 is not its low spin-down power or old age, but the aforementioned geometrical effects.

The optical part of the nonthermal spectrum of PSR B0950+08 also shows an optical efficiency, $\eta_{\text{opt}} \equiv L_{\text{opt}}^{\text{nonth}}/\dot{E}$, much higher than those of the optically detected middle-aged pulsars (Geminga, PSR B0656+14, and Vela), but comparable to those of most powerful, very young pulsars (B0540–69 and Crab). Zharikov et al. (2004) argue that this shows “nonmonotonic evolution” of the optical efficiency and speculate about its physical explanations. However, the \dot{E} dependence of $L_{\text{opt}}^{\text{nonth}}/L_X^{\text{nonth}}$ (where $L_{\text{opt}}^{\text{nonth}}$ is the nonthermal optical luminosity in the 4000–9000 Å band and L_X^{nonth} is that in the 1–10 keV range), plotted in Figure 6 for a sample of seven pulsars (see also Table 2) shows that this ratio remains approximately constant, ~ 0.003 (with a factor of 3 scatter). This means that a more plausible explanation is the same geometrical effect that is responsible for the apparent growth of the X-ray efficiency with age (at $\tau \gtrsim 10 \text{ kyr}$), derived from the very limited sample. This conclusion is further supported by the fact that some old, low- \dot{E} pulsars show quite low X-ray efficiencies, contrary to PSRs B0950+08 and B1929+10 (see § 5.3). The approximately constant value of $L_{\text{opt}}^{\text{nonth}}/L_X^{\text{nonth}}$ suggests a common origin of the magnetospheric X-ray and optical emission and implies similar X-ray and optical beamings.

Finally, we can use the X-ray data to speculate about γ -ray emission of PSR B0950+08. First, we can estimate the maximum photon energy E_{max} up to which the spectral slope can

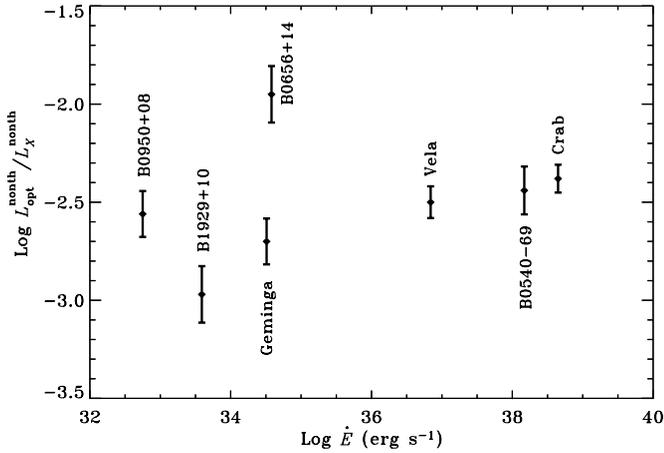


FIG. 6.—Ratio of the nonthermal optical luminosity in the 4000–9000 Å band to the nonthermal component of the X-ray luminosity in the 1–10 keV band vs. spin-down power \dot{E} for seven pulsars. See text and Table 2 for more details.

remain the same as in the optical through X-ray range, from the condition that the total photon luminosity L^{nonth} does not exceed \dot{E} . For example, it gives $E_{\text{max}} < 140$ MeV for the PL model with $\Gamma = 1.35$ discussed in § 4. Next, on the basis of *Compton Gamma Ray Observatory* EGRET observations, Thompson et al. (1994) put an upper limit on the photon flux of PSR B0950+08, $f_{\gamma} < 5.2 \times 10^{-7}$ photons $\text{s}^{-1} \text{cm}^{-2}$ in the 100 MeV – 1 GeV range, a factor of 7 higher than the maximum possible contribution from the PL model of $\Gamma = 1.35$ into this energy range. If, in future observations, γ -ray emission is detected at $E \gtrsim 140$ MeV or the detected γ -ray flux exceeds the extrapolation of the X-ray PL spectrum at $E \lesssim 140$ MeV, it will mean that these γ -rays are generated by a mechanism different from that responsible for the X-ray and optical emission.

5.2. Properties of Polar Caps

Comparison of parameters of heated PCs with the predictions of pulsar models allows one to test these models and better understand the complex physical processes operating in spin-powered pulsars. The PC temperature and radius inferred from the data analysis strongly depend on the assumed model for thermal emission, while the bolometric luminosity is less sensitive to this assumption. For PSR B0950+08, the harder NS atmospheric emission yields a factor of 2 lower surface temperature and a factor of 25 larger emitting area than those obtained with the BB model, whereas the bolometric luminosities are approximately the same, $L_{\text{bol}}^{\text{PC}} \approx 3 \times 10^{29}$ ergs s^{-1} , corresponding to the “PC efficiency” $\eta^{\text{PC}} \equiv L_{\text{bol}}^{\text{PC}} / (2\dot{E}) \approx 2.4 \times 10^{-4}$ (per one polar cap). As we have shown in § 3.2, the assumption that the NS surface is covered with hydrogen leads to a PC radius $R_{\text{PC}} = 160\text{--}340$ m (depending on the pulsar geometry and mass-to-radius ratio) that is in excellent agreement with the conventional estimate, $R_{\text{PC}}^* = (2\pi R^3 / cP)^{1/2} = 288$ m (for $R = 10$ km).

Different pulsar models predict quite different PC luminosities and efficiencies. A detailed analysis of PC heating, relevant to old pulsars, has been recently presented by Harding & Muslimov (2001, 2002, hereafter HM01 and HM02, respectively). They updated the space charge limited flow model (Arons 1981) by including the effects of general relativity on the electric field induced above the NS surface and taking into account inverse Compton scattering (ICS) of thermal X-rays from the NS surface by primary particles (electrons)

TABLE 2
PULSAR LUMINOSITIES

PSR	d (kpc)	$\log \dot{E}$ (ergs s^{-1})	$\log L_{\text{opt}}^{\text{nonth}}$ (ergs s^{-1})	$\log L_X^{\text{nonth}}$ (ergs s^{-1})
Crab.....	2.0	38.65	33.80 ± 0.05	36.18 ± 0.05
B0540–69.....	50.0	38.17	33.94 ± 0.10	36.38 ± 0.07
Vela.....	0.29	36.84	28.80 ± 0.07	31.30 ± 0.04
B0656+14.....	0.29	34.58	28.20 ± 0.12	30.15 ± 0.08
Geminga.....	0.20	34.51	27.49 ± 0.10	30.19 ± 0.06
B1929+10 ^a	0.33	33.59	27.61 ± 0.12	30.58 ± 0.08
B0950+08.....	0.26	32.75	27.36 ± 0.10	29.92 ± 0.06

NOTES.—The fourth and fifth columns give the nonthermal optical (4000–9000 Å) and X-ray (1–10 keV) luminosities computed for the distances given in the second column. The X-ray luminosities of the Crab and Vela pulsars are measured from the *Chandra* observations of 2000 February 2 and 2003 August 20, respectively. For PSR B0950+08, L_X^{nonth} is the luminosity of the PL component in the PL+PC model (§ 3.2), while the luminosities of the other four pulsars are taken from the works of Kaaret et al. (2001; PSR B0540–69), Pavlov et al. (2002; PSR B0656+14), Zavlin & Pavlov (2004; PSR B0656+14 and Geminga), and Wang & Halpern (1997; PSR B1929+10). The optical luminosities are estimated from PL fits of the nonthermal spectral components (a PL extrapolation of the UV spectrum in the case of PSR B1929+10) using the works of Sollerman et al. (2000; Crab), Middleditch et al. (1987; PSR B0540–69), Shibano et al. (2003; Vela), Koptsevich et al. (2001; PSR B0656+14 and Geminga), Mignani et al. (2002; PSR B1929+10), and Zharikov et al. (2004; PSR B0950+08), as well as recent *HST* observations of Vela, PSR B0656+14, and Geminga. The errors for the $L_{\text{opt}}^{\text{nonth}}$ values include our assessment of systematic uncertainties.

^a Since it is assumed that the X-ray emission of B1929+10 is fully non-thermal, while it may have a PC component, the corresponding optical-to-X-ray luminosity ratio can be considered as a lower limit.

accelerated in the NS magnetosphere. In these models, the number of positrons accelerated downward to heat the PC is a tiny fraction of the number of primary electrons that are accelerated upward. The electron-positron pairs are created in the vicinity of the NS surface in cascade processes initiated by γ -ray photons emitted by the primary electrons. HM01 and HM02 calculated the luminosity of a PC heated by positrons produced through curvature radiation (CR) and radiation from ICS. The former process dominates in pulsars with higher magnetic fields and shorter periods. Pulsars with lower fields and longer periods are not capable of producing pairs through CR so that the positrons are produced through less efficient ICS, which results in a lower PC luminosity.

The period and magnetic field of PSR B0950+08 are very close to the boundary between these two regimes (the death line for CR pair production; see Fig. 1 of HM02), so both heating mechanisms should be considered. The PC efficiency and the luminosity of a single PC heated by particles created through CR can be estimated from Figure 7 of HM01 or Figure 9 of HM02: $\eta_{\text{CR}}^{\text{PC}} \approx 10^{-2}$ and $L_{\text{CR}}^{\text{PC}} \approx 6 \times 10^{30}$ ergs s^{-1} , exceeding by a factor of ~ 40 the values we obtained from the spectral analysis. On the other hand, heating through ICS (at $T_{\text{PC}} \sim 1$ MK) gives $\eta_{\text{ICS}}^{\text{PC}} \approx 10^{-5}$ and $L_{\text{ICS}}^{\text{PC}} \approx 6 \times 10^{27}$ ergs s^{-1} (see Figs. 8 and 9 of HM02), a factor of ~ 24 lower than the observational result. This means that either PC heating by ICS-produced positrons is more efficient than calculated by HM02 or, more likely, heating by CR-produced positrons is less efficient in the transition regime near the death line for CR pair production. The CR efficiencies were calculated by HM01 assuming a magnetic inclination angle $\alpha = 60^\circ$; they are expected to decrease with increasing α , approaching $\eta_{\text{CR}}^{\text{PC}} \approx 2 \times 10^{-5} (\tau/17 \text{ Myr})^{1/2} (P/0.253 \text{ s})^{-3/8}$ at $\alpha = 90^\circ$ (eq. [68] of HM01, after correcting the numerical coefficients: $0.7 \rightarrow 0.97$, $0.05 \rightarrow 0.07$, and $3 \rightarrow 0.3$ in the conditions for applicability;

TABLE 3
PROPERTIES OF OLD PULSARS OBSERVED IN X-RAYS

PSR	P (s)	τ (Myr)	$\log \dot{E}$ (ergs s ⁻¹)	d (kpc)	$\log F_X$ (ergs s ⁻¹ cm ⁻²)	$\log L^{\text{nonth}}$ (ergs s ⁻¹)	$\log \eta^{\text{nonth}}$	$\log L_{\text{bol}}^{\text{PC}}$ (ergs s ⁻¹)	$\log \eta^{\text{PC}}$
B2224+65.....	0.683	1.1	33.08	1.86	-13.85	30.87	-2.21	<29.96	<-3.42
J2043+2740 ^a	0.096	1.2	34.75	1.80	-13.96	<30.75	<-4.00	<30.36	<-4.69
B0628-28.....	1.244	2.8	32.45	1.45	-13.27	31.52	-0.93	<30.18	<-2.57
B1813-36.....	0.387	3.0	33.15	2.44	<-14.82	<30.18	<-2.97	<30.44	<-3.01
B1929+10 ^b	0.227	3.1	33.59	0.33	-12.39	30.74	-2.85	30.34	-3.55
B0823+26.....	0.531	4.9	32.65	0.34	<-14.16	<29.00	<-3.65	<29.13	<-3.82
B0950+08.....	0.253	17.4	32.75	0.26	-12.96	30.01	-2.74	29.43	-3.62

NOTES.— Second through fourth columns give standard radio pulsar parameters. The observed (absorbed) fluxes, F_X , nonthermal (isotropic) luminosity, L^{nonth} , and nonthermal X-ray efficiency, $\eta^{\text{nonth}} = L^{\text{nonth}}/\dot{E}$, are for the 0.2–10 keV band. The bolometric PC efficiency is defined as $\eta^{\text{PC}} = L_{\text{bol}}^{\text{PC}}/(2\dot{E})$. The X-ray parameters of PSRs B1813–36 and B1929+10 are from Ögelman & Tepedelenlioğlu (2004) and Wang & Halpern (1997), respectively, whereas those for the other pulsars are from this work. The upper limits on L^{nonth} are derived with a PL model of photon index $\Gamma = 1.5$. The upper limits on $L_{\text{bol}}^{\text{PC}}$ are obtained assuming the conventional PC radius $R_{\text{PC}}^* = 145(P/1\text{ s})^{-1/2}$ m (see § 5.2). The distances to PSRs B1929+10 and 0950+08 are inferred from the pulsars' parallaxes (Briskin et al. 2002). The other distances are estimated from the pulsar dispersion measures and the model of Galactic distribution of free electrons (Cordes & Lazio 2003).

^a The upper limits for PSR J2043+2740 are obtained assuming that the detected thermal X-ray radiation is emitted from the bulk of the NS surface (see § 5.3).

^b The luminosity estimates for PSR B1929+10 are obtained assuming that all the detected X-ray radiation is either nonthermal or thermal.

A. Harding 2004, private communication). This limiting value is a factor of 10 lower than the η^{PC} estimated from the observation, so it seems plausible that the PCs of PSR B0950+08 are heated by CR-produced pairs if α is close to 90°.

Other models of PC heating have been briefly discussed by HM01. As a rule, they predict PC luminosities much higher than those observed (see, e.g., Zavlin & Pavlov 1998), and their applicability to old, low- \dot{E} pulsars is unclear.

5.3. X-Rays from Other Old Pulsars

With the characteristic age of 17 Myr, PSR B0950+08 remains the oldest ordinary pulsar detected outside the radio range, and its spin-down power, $\dot{E} = 5.6 \times 10^{32}$ ergs s⁻¹, is among the lowest in the sample of spin-powered pulsars observed in X-rays. However, there are several old ($\tau \gtrsim 1$ Myr) pulsars, with low spin-down powers ($\dot{E} \lesssim 10^{34}$ ergs s⁻¹), that have been observed in X-rays for sufficiently long time to make a useful comparison with PSR B0950+08. Six such pulsars, in addition to PSR B0950+08, are presented in Table 3, with the relevant pulsar parameters. The X-ray properties of three of them have not been previously reported.

The youngest of the objects included in Table 3 is PSR B2224+65, which powers the Guitar nebula (Cordes et al. 1993). The *Chandra* ACIS¹² observation in 2000 October nicely resolved the pulsar from the nebula. We found that the pulsar's X-ray spectrum (about 80 counts detected in 50 ks) can be described by a PL with $\Gamma = 1.73$ and $L_{2-10\text{ keV}}^{\text{nonth}} = 3.9 \times 10^{30}$ ergs s⁻¹ (the luminosity estimates for this and the other pulsars below are for the distances given in Table 3). Its nonthermal X-ray efficiency, $\eta_{2-10\text{ keV}}^{\text{nonth}} = 0.0033$, exceeds the “maximum efficiency” suggested by Possenti et al. (2002; see § 5.1) by about 40%. Adding to this best fit a hydrogen PC model with $\alpha = \zeta = 45^\circ$, $(M/M_\odot)/(R/10\text{ km}) = 1.4$, $B = 1 \times 10^{12}$ G, and $R_{\text{PC}} = R_{\text{PC}}^* = 145(P/1\text{ s})^{-1/2}$ m (see § 3.2 and § 5.2), we can crudely estimate an upper limit on the PC luminosity (as discussed in § 5.2, the inferred $L_{\text{bol}}^{\text{PC}}$ is almost independent of the assumed model of PC emission). The 1σ upper limit on the PC efficiency of PSR B2224+65, $\eta^{\text{PC}} \sim 4 \times 10^{-4}$, is a factor of 7 lower than the $\eta_{\text{CR}}^{\text{PC}}$ predicted by the HM01 model for $\alpha = 60^\circ$ (as estimated from their Fig. 7 by scaling $\eta_{\text{CR}}^{\text{PC}} \propto P^{3/2}$, according to eq. [67] of HM01).

PSR J2043+27 is of about the same characteristic age as the pulsar B2224+65, but its spin-down power is a factor of 47 higher. Correspondingly, its X-ray properties are quite different. Our analysis of the *XMM-Newton* observation of 2002 November (about 100 source counts in a 12 ks exposure) shows that the pulsar's X-ray emission, detected only at $E \lesssim 2$ keV, is predominantly thermal (a single PL fit yields a photon index $\Gamma \approx 5$, much larger than $\Gamma = 1-2$ for nonthermal X-ray radiation of spin-powered pulsars). The BB fit yields $T_{\text{BB}}^\infty \simeq 0.9$ MK and $R_{\text{BB}}^\infty \simeq 2$ km. The R_{BB}^∞ looks too large compared with the conventional PC radius, $R_{\text{PC}}^* = 470$ m, and the bolometric luminosity, $L_{\text{bol}}^\infty \approx 2 \times 10^{31}$ ergs s⁻¹, is somewhat higher than the maximum value expected from the HM01 model. The NS hydrogen atmosphere models give $T \simeq 0.5$ MK and a radius of emitting area of about 9 km, indicating that the detected X-ray emission originates from the bulk of NS surface. The bolometric surface luminosity in this model is $L_{\text{bol}} \approx 4 \times 10^{31}$ ergs s⁻¹.

The surface temperature of PSR J2043+2740, as yielded by the NS atmosphere fits, is typical for middle-aged pulsars, suggesting that its true age may be smaller than the characteristic age (as one could expect from its short period and high spin-down power). Assuming a photon index $\Gamma = 1.5$ for a possible nonthermal component, we put an upper limit on the nonthermal luminosity, $L_{2-10\text{ keV}}^{\text{nonth}} < 3.8 \times 10^{30}$ ergs s⁻¹, such that the X-ray efficiency, $\eta_{2-10\text{ keV}}^{\text{nonth}} < 6.8 \times 10^{-5}$, is a factor of 20 lower than that of PSR B0950+08, and it is a factor of 200 lower than the maximum efficiency for this \dot{E} . Assuming that the detected thermal emission is due to NS cooling, the upper limit on PC efficiency is the lowest among those found for the other pulsars in Table 3. However, this result should be taken with caution, given the small number of counts detected and strong correlation between the properties of the two possible thermal components. A deeper observation is required to constrain the parameters with better certainty.

The 2.8 Myr old pulsar B0628–28 is the most puzzling object of this group because it was found to be extremely luminous in the X-ray domain (Ögelman & Tepedelenlioğlu 2004). Our analysis of the 20 ks ACIS data of 2001 November shows that the source spectrum is best fitted with a PL model of $\Gamma = 2.73$, which is surprisingly steep for a spin-powered pulsar. The estimated X-ray efficiency in the 2–10 keV range is about 0.015, much higher than for any other spin-powered pulsar detected in X-rays, and it is well above the maximum

¹² Advanced CCD Imaging Spectrometer.

efficiency discussed in § 5.1. Single-component thermal models fail to give statistically acceptable fits of the observed spectrum (e.g., the best BB fit yields $\chi^2_\nu = 4.4$ for 9 dof). Further analysis of this source, including optical observations, is needed to confirm that this is indeed the pulsar counterpart.

Another 3 Myr old pulsar, B1813–36, was not detected in a 30 ks *Chandra* ACIS exposure of 2001 October (Ögelman & Tepedelenlioglu 2004). An upper limit on its X-ray efficiency, $\eta_{2-10\text{ keV}}^{\text{nonth}} < 4.4 \times 10^{-4}$, is a factor of 2.5 lower than that for PSR B0950+08. The upper limit on PC luminosity is very close to that predicted by the HM01 results.

PSR B1929+10 has about the same age as the two previous pulsars, but it is much closer. Its X-ray luminosity was estimated from an *ASCA* observation (Wang & Halpern 1997). Assuming that the detected emission is nonthermal, the pulsar’s luminosity is $L_{2-10\text{ keV}}^{\text{nonth}} \simeq 2.1 \times 10^{30}$ ergs s⁻¹, or 5.5×10^{-4} of the spin-down power, for $d = 330$ pc derived by Brisken et al. (2002) from the pulsar’s parallax (another estimate, $d \simeq 360$ pc, obtained by Chatterjee et al. 2004, increases the luminosity and efficiency by about 20%). The optical radiation of this pulsar (Pavlov et al. 1996; Mignani et al. 2002) is most likely of a nonthermal origin, with an optical efficiency close to that of PSR B0950+08. The same *ASCA* spectrum could be interpreted as thermal (BB) emission from pulsar’s PCs of a temperature of about 0.5 MK, radius $R_{\text{BB}}^\infty \simeq 600$ m, and bolometric luminosity of 2.2×10^{30} ergs s⁻¹ (for $d = 330$ pc). The corresponding efficiency of one PC, $\eta^{\text{PC}} = 2.8 \times 10^{-4}$, is very close to that of PSR B0950+08, and it is a factor of 7 lower than $\eta_{\text{CR}}^{\text{PC}}$ estimated from Figure 7 of HM01. The difference is not as large as for PSR B0950+08, but we should not forget that the actual η^{PC} may be lower than obtained from the BB fit if the contribution of the nonthermal component is not negligible. New data on PSR B1929+10 collected with *XMM-Newton* in 2003 October and 2004 April are expected to determine the origin of its X-ray emission and measure the contributions of the thermal and nonthermal components.

Another nearby old pulsar, B0823+26, was observed with *XMM-Newton* in 2002 April, but the pulsar was only marginally detected, at a count rate of 0.003 ± 0.001 counts s⁻¹ in the effective EPIC-pn exposure of 34 ks. We conservatively consider this as an upper limit until the detection is confirmed with another observation. We estimated an upper limit on the nonthermal X-ray luminosity: $L_{2-10\text{ keV}}^{\text{nonth}} < 6.0 \times 10^{28}$ ergs s⁻¹ for a PL photon index $\Gamma = 1.5$. The corresponding upper limit on the nonthermal efficiency, $\eta_{2-10\text{ keV}}^{\text{nonth}} < 1.3 \times 10^{-4}$, is at least a factor of 10 smaller than the efficiency found for PSR B0950+08, and a factor of 6 smaller than for PSR B1929+10, whose \dot{E} and τ are very close to those of PSR B0823+26. The upper limit on η^{PC} is a factor of 70 lower than the estimate for $\eta_{\text{CR}}^{\text{PC}}$ obtained from Figure 7 of HM01, but it is 3 orders of magnitude higher than $\eta_{\text{ICS}}^{\text{PC}}$ obtained from Figure 8 of HM02.

Thus, the analysis of this sample of old pulsars shows quite different properties of X-ray emission. The most powerful PSR J2043+2740 manifests itself as a cooling NS, similar to middle-aged pulsars. Some of the pulsars (J2043+2740, PSR B0823+26) show rather low upper limits on the nonthermal X-ray efficiency, which means that not all old pulsars are as X-ray efficient as PSR B0950+08. On the other side, the X-ray efficiency of PSR B2224+65 is higher than those of PSR B0950+08 and PSR B1929+10, while PSR B0628–28 apparently shows an extremely high efficiency, well above the maximum expected value.

The nearest pulsars in this sample, B0950+08 and B1929+10, show evidence of PC emission, with bolometric luminosities $L_{\text{bol}}^{\text{PC}} \sim 3 \times 10^{29}$ and $\leq 2 \times 10^{30}$ ergs s⁻¹, respectively. The upper limits on $L_{\text{bol}}^{\text{PC}}$ derived for the other pulsars are in the range $(1-30) \times 10^{29}$ ergs s⁻¹. For all the pulsars except for the most distant (and strongly absorbed) B1813–36, the estimated efficiencies (or upper limits) fall below the model predictions of HM01 for $\eta_{\text{CR}}^{\text{PC}}$ (B0823+26 being particularly “underheated”), but they are well above the predictions of HM02 for $\eta_{\text{ICS}}^{\text{PC}}$. Since most of these pulsars, except for J2043+2740, are close to (or slightly above) the “CR death line,” it hints that the model of HM01 may need a revision for such pulsars.

6. SUMMARY

The *XMM-Newton* observation of the old pulsar PSR B0950+08 allowed us to investigate its timing and spectral properties in X-rays. The timing analysis revealed the pulsations of the X-ray flux, with the pulse shape and pulsed fraction depending on photon energy. At $E \gtrsim 0.5$ keV the observed light curve shows two relatively narrow peaks with a high pulsed fraction, $\approx 60\%$, which is a strong indication of a nonthermal (magnetospheric) origin of the X-ray emission. The light curve extracted at lower energies shows a broad single pulse with a lower pulsed fraction. This energy dependence can be explained by the presence of another, most likely thermal, component.

The spectral analysis of the detected X-ray radiation supports this interpretation. The X-ray spectrum of PSR B0950+08 can be described by a two-component, thermal plus nonthermal model. We suggest that the thermal component is emitted from two hot ($T \approx 1$ MK) spots (PCs) around the pulsar magnetic poles, covered by a hydrogen atmosphere. Its spectrum peaks at lower energies, which can explain the energy dependence of the X-ray pulse profiles. The PC radius, $R_{\text{PC}} \approx 250$ m, estimated from the magnetized NS hydrogen atmosphere models, is in good agreement with the predictions of the pulsar models. This PC model is consistent with the inferred light curve of the thermal component at reasonable values of pulsar parameters. The PC luminosity, $L_{\text{bol}}^{\text{PC}} \approx 3 \times 10^{29}$ ergs s⁻¹, is in agreement with the model by HM01 for PC heating by positrons generated by CR if the spin and magnetic axes of the pulsar are nearly orthogonal.

The two-component interpretation of the X-ray emission combined with the fluxes measured in five optical-UV bands implies that the spectral slope of the magnetospheric component remains the same, $\Gamma = 1.35 \pm 0.05$, in a broad energy range, from 1 eV to 10 keV, and the magnetospheric luminosity and efficiency are about 1×10^{30} and 2×10^{-3} ergs s⁻¹ in this energy range. Both X-ray and optical magnetospheric emission of PSR B0950+08 look more luminous than expected from extrapolations of empirical $L\text{-}\dot{E}$ correlations derived for younger, more powerful pulsars. However, the X-ray-to-optical luminosity ratio is about the same as that for other pulsars observed in both the X-ray and optical. This implies a close connection between (possibly the same mechanism for) the optical and X-ray magnetospheric emission, while the fact that PSR B0950+08 is apparently “overluminous” in comparison with some (but not all) younger pulsars is associated with geometrical effects (beaming of radiation and orientations of pulsar axes) that are also responsible for the large scatter in the $L_X\text{-}\dot{E}$ correlation.

The comparison of PSR B0950+08 with six other old pulsars observed in X-rays reveals very diverse properties of the X-ray spectra and luminosities of old pulsars. In particular, the

estimated magnetospheric X-ray efficiencies of these pulsars vary from $<10^{-4}$ to $\sim 10^{-1}$. The large scatter in a narrow range of characteristic ages (or spin-down powers) confirms that some “hidden” parameters (e.g., orientations of the pulsar’s axes) affect the apparent X-ray luminosities of pulsars. Most of the PC luminosities (or their upper limits) estimated for this group of pulsars fall below the model predictions for PC heating by relativistic particles produced through CR, indicating that the models may require a revision for pulsars near the “death line” for this pair production mechanism.

Finally, the derived upper limit of 0.15 MK on the NS brightness temperature in the optical-UV range (for a standard

NS radius) constrains heating mechanisms possibly operating in the NS interiors. The actual temperature (or a more restrictive upper limit) can be measured from far-UV observations of PSR B0950+08.

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Note added in proof.—After this paper was submitted for publication, we became aware of the work by W. Becker et al. (*ApJ*, in press [2004]), who analyzed the same data on PSR B0950+08. They considered only the power-law interpretation of the pulsar’s spectrum and obtained fitting parameters in fair agreement with our results for this fit.